

### Math 125 Final Exam, Fall 2015

- The following exam has 4 parts, 21 problems, and 8 pages. Please stop and make sure that your exam has all its pages.
- Please raise your hand if you have any questions or need a restroom break.
- When you have completed your exam, raise your hand and the instructor will collect your exam. DO NOT begin packing up until you have turned your exam in.
- ANY use of cell phones or electronics other than an appropriate calculator will result in you receiving a zero on your final exam.
- ANY cheating (cheat sheets, communicating with classmates, etc.) will result in you receiving a zero on your final exam.

**Section 1: Quick problems.** Show work to receive partial credit. Make sure you simplify fully and round appropriately.

1. [5] Complete the indicated operation and give your answer in scientific notation. Round appropriately as your final step:

a.  $2.1 \times 10^{-3} + 7.1 \times 10^{-4}$

2. [5] Simplify. Express results with positive exponents only:

a.  $\left(\frac{3x^{-2}}{y^5}\right)^{-3}$

3. [7] Perform the indicated operations and simplify. Be sure to write your answer in the correct form:

a.  $(4x^2 - 1 + 8x) \div (2x + 3)$

4. [15] Factor each polynomial completely:

a.  $3x^2 - 20x + 12$

b.  $x^4 - 16$

c.  $27x^3 + 8$

5. [5] Perform the indicated operation and simplify:

a.  $(4 - 3i)(i - 2)$

6. [5] Simplify and solve for x. Give an exact answer:

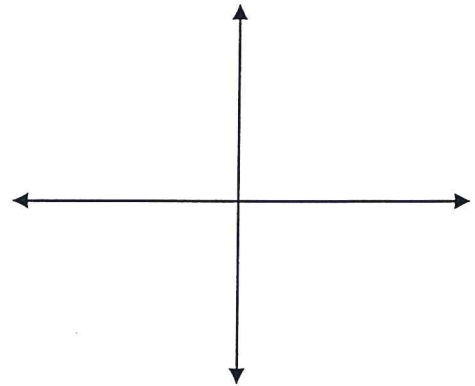
a.  $x = \log_3 27$

**Section 2: Graphing and calculations.** Show all work to receive credit. Be sure to simplify.

7. [9] Considering the following function:  $f(x) = \sqrt{2-x}$

a. Find the domain of  $f(x)$ :

b. Graph  $f(x)$  and label at least three points including the x-intercept:



8. [10] Give the equation of the line in slope-intercept form which is perpendicular to the line  $2x-3y=5$  and passes through the point  $(1,3)$ .

9. [8] Solve the system of equations:

a. 
$$\begin{aligned} 4x - 9y &= 5 \\ 3x + 12y &= 10 \end{aligned}$$

10. [6] If  $y$  varies directly with  $x^2$  and  $y=6$  when  $x=3$ , find  $y$  when  $x=5$ . Give an exact answer:

11. [6] Perform the indicated operations, factor, and reduce the following to simplest form. You may leave your answer in factored form:

a. 
$$\left(\frac{x^2-16}{x}\right) \div \left(\frac{x^2+3x-4}{7x^2-14x}\right)$$

12. [20] Solve the following equations for  $x$ . Give exact answers:

a.  $\frac{1}{x} - \frac{3}{2x+6} = \frac{5}{2x}$

b.  $K = \frac{ax}{x+b}$

c.  $x^2 + 6x = -3$

**Section 3: Word problems.** Show all work to receive credit. Be sure to use appropriate rounding and include units!

13. [12] Erica can paddle at a rate of 5.0 mph in still water. Paddling downstream, she pulls up to her favorite fishing hole in 1 hour and 20 minutes. If the return trip upstream takes 5 hours, what is the average rate of the river? Round to two decimal places.
14. [12] How many liters of a 25% acid solution must be mixed with a 12% acid solution to produce 5 liters of a 20% acid solution? Round to one decimal place.
15. [10] A bird is perched at the top of a tree. On the ground he sees a worm. If the tree is 28.0 feet tall and the angle of depression from the bird to the worm is  $54.0^\circ$ , how far is the worm from the base of the tree? Round appropriately.

**Section 4: Geometry and Trig.** Show all work to receive credit. Round appropriately or as indicated in the problem.

16. [10] Find the area of the following:
- The area between a circle and an inscribed square where the circle has radius 18.0 in. Round to three significant digits.
17. [12] Given the three parts of a triangle, find the remaining three parts. You may round off the length of sides to three significant digits and round off angles to the nearest  $1/10$  of a degree.
- $C=90.0^\circ$ ,  $A=47.0^\circ$ ,  $c=14.0$  ft
18. [12] Find the area of a regular pentagon with perimeter of 84.0 feet.

19. [8] Find the measure of the central angle in degrees for a sector of a circle that has a radius of 1.50 inches and an arc length of 1.68 inches. Round to three significant digits.

20. [15] Given  $a=8150\text{m}$ ,  $b=3250\text{m}$ ,  $C = 27.8^\circ$ , find the three remaining parts of an oblique triangle. You may round off the length of sides to the correct number of significant figures and round off angles to the nearest  $1/10$  of a degree:

Hint: Law of Sines:  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ , Law of Cosines: 
$$\begin{cases} a^2 = b^2 + c^2 - 2bc(\cos A) \\ b^2 = a^2 + c^2 - 2ac(\cos B) \\ c^2 = a^2 + b^2 - 2ab(\cos C) \end{cases}$$

21. [8] Sketch a graph of  $f(x) = 2\cos x$ . Be sure to show at least one full period. Label the y-intercept and three other points.