
*SHOW ALL WORK**Keep three decimal places in most calculations*

1. The ages of people in a group (to the nearest year) are as follows:

18 23 18 21 19 25 33 51

- (a) [7] Find the sample mean and standard deviation of the ages.

- (b) [10] Find the Five Number Summary

- (c) [5] Is there any outlier in this data set? If any, which value? Use 1.5 IQR rule.

2. In Spring 1999 the grade distribution for Math 282 is recorded below. Other stands for withdrawals, incompletes, etc.

grade	A	B	C	D	F	Other
probability	?	0.282	0.113	0.070	0.014	0.085

- (a) [3] What is the probability that a randomly selected Math 282 student received a grade of an A?

- (b) [3] What is the probability that a randomly selected Math 282 student received a grade of an A or B?

3. The scores of students on the ACT in 2001 had a normal distribution with mean $\mu = 23$ and standard deviation $\sigma = 4.7$.

(a) [5] What is the probability that a randomly chosen student has the test score 21 or higher?

(b) [5] How high must be the score of a student to be on the top of 10%.

c) [6] Consider an SRS of 9 students who took the test. Find $P(21 < \bar{X} < 27)$.

4. Emily hits 60% of her free throws in basketball games. This year she had 45 free throws.

(a) [6] Find the mean and standard deviation of the number of hits.

(b) [6] Use the normal approximation to find the probability that she made at least 30 hits this year?

5. [8] If we want to estimate p , the population proportion of likely voters that believe the economy state is the most urgent national concern with 99% confidence and a margin of error no greater than 3%, how many likely voters need to be surveyed? Assume that you have no idea of the value of p .
6. Suppose it is desired to predict the weight of the human brain from a measurement of head size. The correlation $r = 0.6719$.

variable	mean	standard deviation
brain weight	1263.2	164.5
head size	15.174	0.8862

- (a) [8] Find the intercept and slope of the least square line
- (b) [8] Write the regression line and use it to predict the response variable when $x = 16.2$
7. A researcher has developed a new drug designed to reduce blood pressure. In an experiment, 21 subjects were assigned randomly to the treatment group, and received the new experimental drug. The other 23 subjects were assigned to the control group, and received a standard, well known treatment. After a suitable period of time, the reduction in blood pressure for each subject was recorded. A summary of these data is:

	n	Mean	Stdev
new drug	21	23.48	8.01
old drug	23	18.52	7.15

- (a) [12] Do the appropriate 4 step test. (Let $\alpha = .05$)

(b) [10] Find a 96% confidence interval for difference between two group means.

8. A physiology student believed that caffeine would increase the amount of potassium in the urine. Seven students measured the amount of potassium in their urine after taking a caffeine pill (μ_1) and before taking the pill (μ_2). Assume that the appropriate procedure can be used. The output below is the data collected from the seven students. Let $\mu_d = \mu_1 - \mu_2$

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test          alternative    T-value p-value 95% CI for mud=mu1-mu2:
matched pairs: mud not = 0   2.51    0.066   (-0.0095, 0.1906)
matched pairs: mud    > 0   2.51    0.033   (-0.0095, 0.1906)
matched pairs: mud    < 0   2.51    0.967   (-0.0095, 0.1906)
2 sample t      : mu1 not = mu2 1.64    0.15    (-0.040, 0.221)
2 sample t      :      mu1 > mu2 1.64    0.073   (-0.040, 0.221)
2 sample t      :      mu1 < mu2 1.64    0.93    (-0.040, 0.221)

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(a) [5] Which procedure should be used? Explain briefly.

(b) [12] Do a 4 step test of hypotheses.

(c) [5] Give a 95% confidence interval for the difference in mean amount of potassium.

9. Find the p-value (exactly for the normal distribution, and a range for the t distribution) in each of the following hypothesis testing problems:
- (a) [5] Testing $\mu = 10$ versus $H_a : \mu < 10$; sample size $n = 25$, test statistic $z = -2.11$.
- (b) [5] Testing $\mu = 10$ versus $H_a : \mu \neq 10$; sample size $n = 10$, test statistic $t = 2.8$ (Assume normal distribution of the population)
10. The table below is a SRS of 1000 people from a community hospital. A new flu vaccine was provided free of charge in a two shot sequence over a period of two weeks. Some people received the two shot sequence, some appeared for one shot, and others received neither. It is desired to test whether there was any relationship between the number of flu shots and whether a person gets the flu.

		No Shot	One Shot	Two Shots	total
Flu	observed	24	9	13	46
	expected	(14.40)	(5.01)	(26.59)	
	cell chisq	[6.404]	[3.169]	[6.944]	
No Flu	observed	289	100	565	954
	expected	()	(103.99)	(551.41)	
	cell chisq	[]	[0.153]	[]	
total		313	109	578	1000

- a) [12] Find the value of the expected count that is not given in the table. Find the 2 cell chi square contributions that need to be computed. Show work.

- b) [12] Do a 4 step of hypotheses. Show how the appropriate table is used ($\alpha = 0.05$)

11. [12] In a random sample of 500 people aged 20-24, 22% were smokers. In a random sample of 450 people aged 25-29, 14% were smokers. Construct a 95% confidence interval for the difference between the population proportions $p_1 - p_2$.
12. [30] Circle the correct answer
- (I) Which of the following is least affected if an extreme high outlier is added to the data:
- a) the median b) the mean c) the standard deviation
- (II) The distribution of SAT math scores was Normal with mean 516 and standard deviation 116, the distribution of ACT math scores was Normal with mean 21.0 and standard deviation 5.3. Alysha scored 680 on SAT. John scored 18.8 on ACT. Assume that both tests measure the same kind of ability, who had the higher score?
- a) Alysha b) John c) same
- (III) Which of the following correlation indicates the strongest relationship?
- a) $r = 0.8$ b) $r = 0.09$ c) $r = -0.85$
- (IV) In a Venn diagram two events A and B are not overlapping. This means they are independent
- a) true b) false
- (V) A market researcher selects 500 drivers under 30 years of age and 500 drivers over 30 years of age. Identify the type of sampling is used
- a) Cluster b) Systematic c) Stratified d) Random e) Convenience
- (VI) A researcher interviews 19 work colleagues who work in his building. Identify the type of sampling is used
- a) Cluster b) Systematic c) Stratified d) Random e) Convenience

(VII) The number of oil spills occurring off the Alaskan coast is a

- a) Continuous random variable b) Discrete random variable

(VIII) The height of a randomly selected student is a

- a) Continuous random variable b) Discrete random variable

(IX) If the 95% confidence interval is 60.0 to 70.0, then we can safely conclude that

a) the sample mean is within that interval 95% of the time.

b) the population mean is within that interval 95% of the time.

c) the mean of the population is 95.

d) if we collected 20 different samples with same size, and made twenty 95% confidence intervals from the 20 samples, that approximately 19 of those confidence intervals would contain the population mean, and about 1 would not.

(X) Let A and B be two events and $P(A)=0.3$, $P(B)=0.6$ and $P(A \text{ and } B)=0.2$. $P(A \text{ or } B)$ is equal:

- a) 0.9 b) 0.7 c) 0.18 d) 0.8

Formulas

$$\bar{x} = \frac{\sum x}{n} \quad s^2 = \frac{\sum (x - \bar{x})^2}{n-1} \quad z\text{-score} = \frac{\text{value} - \text{mean}}{\text{standard deviation}} \quad IQR = Q_3 - Q_1$$

$$\text{confidence interval} \quad \bar{x} \pm z^* \frac{\sigma}{\sqrt{n}}, \quad \bar{x} \pm t^* \frac{s}{\sqrt{n}}, \quad \text{sample size} \quad n = \left(\frac{z^* \sigma}{m}\right)^2$$

$$\text{test statistics} \quad z = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}, \quad t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$$

two sample confidence interval and test statistics

$$(\bar{x}_1 - \bar{x}_2) \pm z^* \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}, \quad (\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}, \quad z = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}, \quad t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$\text{Proportion problems: } \hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \quad n = \left(\frac{z^*}{m}\right)^2 p^* (1 - p^*)$$

Proportion problems for two populations:

$$(\hat{p}_1 - \hat{p}_2) \pm z^* \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} \quad z = \frac{(\hat{p}_1 - \hat{p}_2)}{\sqrt{\hat{p}(1-\hat{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad \hat{p} = \frac{x_1 + x_2}{n_1 + n_2}$$

Regression:

$$r = \frac{1}{n-1} \sum \left(\frac{x-\bar{x}}{s_x}\right) \cdot \left(\frac{y-\bar{y}}{s_y}\right) = \frac{1}{n-1} \sum Z_x \cdot Z_y, \quad \hat{y} = a + bx \quad \text{where } b = r \frac{s_y}{s_x}, \text{ and } a = \bar{y} - b\bar{x}$$

Chi-Square Testing:

$$\chi^2 = \sum \frac{(\text{Obs.} - \text{Exp.})^2}{\text{Exp.}}, \text{ where } \text{Exp.} = \frac{(\text{row total})(\text{column total})}{\text{overall total}}, \text{ and } df = (r-1)(c-1)$$

Table entry for C is the critical value t^* required for confidence level C. To approximate one- and two-sided F -values, compare the value of the t statistic with the critical values of t^* that match the P -values given at the bottom of the table.

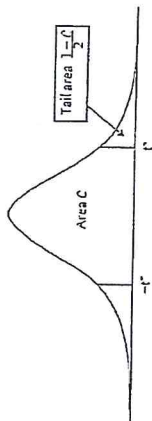


TABLE C t DISTRIBUTION CRITICAL VALUES

DEGREES OF FREEDOM	CONFIDENCE LEVEL C																
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%	99.9%	99.9%	99.9%	99.9%	
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6	636.6	636.6	636.6	636.6	636.6
2	0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60	31.60	31.60	31.60	31.60	31.60
3	0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92	12.92	12.92	12.92	12.92	12.92
4	0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610	8.610	8.610	8.610	8.610	8.610
5	0.727	0.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869	6.869	6.869	6.869	6.869	6.869
6	0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959	5.959	5.959	5.959	5.959	5.959
7	0.711	0.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408	5.408	5.408	5.408	5.408	5.408
8	0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.898	3.355	3.833	4.501	5.041	5.041	5.041	5.041	5.041	5.041
9	0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781	4.781	4.781	4.781	4.781	4.781
10	0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587	4.587	4.587	4.587	4.587	4.587
11	0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437	4.437	4.437	4.437	4.437	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318	4.318	4.318	4.318	4.318	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221	4.221	4.221	4.221	4.221	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140	4.140	4.140	4.140	4.140	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.603	2.947	3.286	3.733	4.073	4.073	4.073	4.073	4.073	4.073
16	0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015	4.015	4.015	4.015	4.015	4.015
17	0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965	3.965	3.965	3.965	3.965	3.965
18	0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922	3.922	3.922	3.922	3.922	3.922
19	0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883	3.883	3.883	3.883	3.883	3.883
20	0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850	3.850	3.850	3.850	3.850	3.850
21	0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819	3.819	3.819	3.819	3.819	3.819
22	0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792	3.792	3.792	3.792	3.792	3.792
23	0.685	0.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768	3.768	3.768	3.768	3.768	3.768
24	0.685	0.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745	3.745	3.745	3.745	3.745	3.745
25	0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725	3.725	3.725	3.725	3.725	3.725
26	0.684	0.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707	3.707	3.707	3.707	3.707	3.707
27	0.684	0.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690	3.690	3.690	3.690	3.690	3.690
28	0.683	0.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674	3.674	3.674	3.674	3.674	3.674
29	0.683	0.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659	3.659	3.659	3.659	3.659	3.659
30	0.683	0.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.646	3.646	3.646	3.646	3.646	3.646
40	0.681	0.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551	3.551	3.551	3.551	3.551	3.551
50	0.679	0.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496	3.496	3.496	3.496	3.496	3.496
60	0.679	0.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460	3.460	3.460	3.460	3.460	3.460
80	0.678	0.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416	3.416	3.416	3.416	3.416	3.416
100	0.677	0.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390	3.390	3.390	3.390	3.390	3.390
1000	0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300	3.300	3.300	3.300	3.300	3.300
z^*	0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291	3.291	3.291	3.291	3.291	3.291
One-sided P	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005	.0005	.0005	.0005	.0005	.0005
Two-sided P	.50	.40	.30	.20	.10	.05	.04	.02	.01	.005	.0025	.001	.001	.001	.001	.001	.001

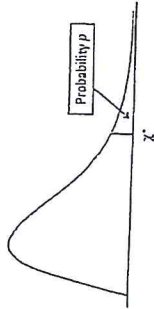


Table entry for p is the critical value x^* with probability p lying to its right.

TABLE D CHI-SQUARE DISTRIBUTION CRITICAL VALUES

df	P																
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005	.0005	.0005	.0005	.0005	
1	1.32	1.64	2.07	2.71	3.84	5.02	5.41	6.63	7.88	9.14	10.83	12.12	12.12	12.12	12.12	12.12	12.12
2	2.77	3.22	3.79	4.61	5.99	7.38	7.82	9.21	10.60	11.98	13.82	15.20	15.20	15.20	15.20	15.20	15.20
3	4.11	4.64	5.32	6.25	7.81	9.35	9.84	11.34	12.84	14.32	16.27	17.73	17.73	17.73	17.73	17.73	17.73
4	5.39	5.99	6.74	7.78	9.49	11.14	11.67	13.28	14.86	16.42	18.47	20.00	20.00	20.00	20.00	20.00	20.00
5	6.63	7.29	8.12	9.24	11.07	12.83	13.39	15.09	16.75	18.39	20.51	22.11	22.11	22.11	22.11	22.11	22.11
6	7.84	8.56	9.45	10.64	12.59	14.45	15.03	16.81	18.55	20.25	22.46	24.10	24.10	24.10	24.10	24.10	24.10
7	9.04	9.80	10.75	12.02	14.07	16.01	16.62	18.48	20.28	22.04	24.32	26.02	26.02	26.02	26.02	26.02	26.02
8	10.22	11.03	12.03	13.36	15.51	17.53	18.17	20.09	21.95	23.77	26.12	27.87	27.87	27.87	27.87	27.87	27.87
9	11.39	12.24	13.29	14.68	16.92	19.02	19.68	21.67	23.59	25.46	27.88	29.67	29.67	29.67	29.67	29.67	29.67
10	12.55	13.44	14.53	15.99	18.31	20.48	21.16	23.21	25.19	27.11	29.59	31.42	31.42	31.42	31.42	31.42	31.42
11	13.70	14.63	15.77	17.28	19.68	21.92	22.62	24.72	26.76	28.73	31.26	33.14	33.14	33.14	33.14	33.14	33.14
12	14.85	15.81	16.99	18.55	21.03	23.34	24.05	26.22	28.30	30.32	32.91	34.82	34.82	34.82	34.82	34.82	34.82
13	15.98	16.98	18.20	19.81	22.36	24.74	25.47	27.69	29.82	31.88	34.53	36.48	36.48	36.48	36.48	36.48	36.48
14	17.12	18.15	19.41	21.06	23.68	26.12	26.87	29.14	31.32	33.43	36.12	38.11	38.11	38.11	38.11	38.11	38.11
15	18.25	19.31	20.60	22.31	25.00	27.49	28.26	30.38	32.80	34.95	37.70	39.72	39.72	39.72	39.72	39.72	39.72
16	19.37	20.47	21.79	23.54	26.30	28.85	29.63	32.00	34.27	36.46	39.25	41.31	41.31	41.31	41.31	41.31	41.31
17	20.49	21.61	22.98	24.77	27.59	30.19	31.00	33.41	35.72	37.95	40.79	42.88	42.88	42.88	42.88	42.88	42.88
18	21.60	22.76	24.16	25.99	28.87	31.53	32.35	34.81	37.16	39.42	42.31	44.43	44.43	44.43	44.43	44.43	44.43
19	22.72	23.90	25.33	27.20	30.14	32.85	33.69	36.19	38.58	40.88	43.82	45.97	45.97	45.97	45.97	45.97	45.97
20	23.83	25.04	26.50	28.41	31.41	34.17	35.02	37.57	40.00	42.34	45.31	47.50	47.50	47.50	47.50	47.50	47.50
21	24.93	26.17	27.66	29.62	32.67	35.48	36.34	38.93	41.40	43.78	46.80	49.01	49.01	49.01	49.01	49.01	49.01
22	26.04	27.30	28.82	30.81	33.92	36.78	37.66	40.29	42.80	45.20	48.27	50.51	50.51	50.51	50.51	50.51	50.51
23	27.14	28.43	29.98	32.01	35.17	38.08	38.97	41.64	44.18	46.62	49.73	52.00	52.00	52.00	52.00	52.00	52.00
24	28.24	29.55	31.13	33.20	36.42	39.36	40.27	42.98	45.56	48.03	51.18	53.48	53.48	53.48	53.48	53.48	53.48
25	29.34	30.68	32.28														