## MATH 150 – TOPIC 10 ARC LENGTH AND RADIAN MEASURE

Consider a circle of radius r centered at the origin. Then the angle  $\theta$ , measured in radians (see Review Topic 8), subtends (or "marks off") an arc of length s on the circle. For one complete revolution, which is  $2\pi$  radians, the corresponding arc length is the circumference of the circle,  $2\pi r$ . Using proportions, we have

or

or



| angle                           | one revolution          |
|---------------------------------|-------------------------|
| $\frac{1}{\text{arc length}} =$ | circumference,          |
| $\frac{\theta}{s} =$            | $=\frac{2\pi}{2\pi r},$ |

 $s = r\theta$ , where  $\theta$  is in radians.

The importance of this formula will be seen in Review Topic 1.

PRACTICE PROBLEMS for Topic 10 – Arc Length and Radian Measure

10.1 If  $\theta = \frac{\pi}{2}$  and r = 2, how long is the arc length subtended?

10.2 On a circle whose radius is 3, what angle subtends an arc of length 4?

## ANSWERS to PRACTICE PROBLEMS (Topic 10 – Arc Length and Radian Measure)

10.1  $\pi$  units 10.2  $\frac{4}{3}$  radians

Beginning of Topic

Skills Assessment